

- (27) Pitzer, K. S., Lippmann, D. Z., Curl, R. F., Huggins, C. M., Peterson, D. E., *ibid.*, p 3433.
- (28) Prengle, H. W., Greenhaus, L. R., York, Jr., R., *Chem. Eng. Progr.*, **44**, 863 (1948).
- (29) Sage, B. H., Webster, D. C., Lacey, W. N., *Ind. Eng. Chem.*, **29**, 118 (1937).
- (30) Seibert, F. M., Burrell, G. A., *J. Amer. Chem. Soc.*, **37**, 2683 (1915).
- (31) "Selected Values of Properties of Hydrocarbons and Related Compounds," API Research Project 44, Thermodynamics Research Center, Texas A&M University, College Station, Tex. (loose-leaf data sheets, extant, 1971).
- (32) Sliwinski, P., *Z. Phys. Chem. (Frankfurt am Main)*, **63**, 263 (1969).
- (33) Technical Committee, National Gasoline Association of America, *Ind. Eng. Chem.*, **34**, 1240 (1942).
- (34) Visser, S. W., dissertation, University of Leiden, The Netherlands, 1913.
- (35) Wackher, R. C., Linn, C. B., Grosse, A. V., *Ind. Eng. Chem.*, **37**, 464 (1945).
- (36) Wilhoit, R. C., Hathaway, A. W., Table of Conversion Factors Based on Accepted Constants As of 1965, Report of Investigation, API Research Project 44, Thermodynamics Research Center, Texas A&M University, College Station, Tex., 1965.
- (37) Young, S., *Proc. Roy. Irish Acad.*, **38 B4**, 65 (1928).

Received for review November 22, 1972. Accepted April 2, 1973. The support of the American Petroleum Institute Research Project 44 of the Thermodynamics Research Center is acknowledged, together with that of Texas Engineering Experiment Station, both of Texas A&M University. **Supplementary Material Available.** The complete Table VIII will appear following these pages in the microfilm edition of this volume of the journal. Photocopies of the supplementary material from this paper only or microfiche (105 X 148 mm, 20X reduction, negatives) containing all of the supplementary material for the papers in this issue may be obtained from the Journals Department, American Chemical Society, 1155 16th St., N.W., Washington, D.C. 20036. Remit check or money order for \$3.00 for photocopy or \$2.00 for microfiche, referring to code number JCED-73-244.

PVT Surface and Thermodynamic Properties of Isobutane

Tarun R. Das and Charles O. Reed, Jr.

Department of Chemistry and Thermodynamics Research Center, Texas A&M University, College Station, Tex. 77843

Philip T. Eubank¹

Department of Chemical Engineering and Thermodynamics Research Center, Texas A&M University, College Station, Tex. 77843

Selected values of vapor pressure, specific volume, enthalpy, and entropy are presented for the saturated liquid and vapor states of isobutane from the normal boiling point (261.32K) to the critical point (408.13K). Experimental values of the density, together with the saturated vapor densities, were fitted to a differential regional Benedict-Webb-Rubin (DR-BWR) equation of state; compressibility factors were generated from 270 to 600K with pressure to 400 atm. Thermodynamic properties of the real gas, $H - H^\circ$, $(H - H^\circ)/T$, $A - A^\circ$, $S - S^\circ$, $S - S^l$, $G - G^\circ$, $(G - G^\circ)/T$, $G - G^l$, and f/P , were also calculated from the classical relationships. These results illustrate the inconsistency of different experimental data sets for isobutane and the need for new density and enthalpy data.

A number of correlation studies (6, 12, 28) present both vapor-liquid coexistence and superheated vapor thermodynamic properties of isobutane. The present compilation is part of a general revision of the j-tables of real gas properties of the API Research Project 44 (30) for C₁-C₅ alkanes.

Physical Constants

Table I is a list of the physical conversion constants (35) used in this investigation. A summary of selected, experimentally determined, critical constants is shown in Table II. The present set of critical constants ($T_c = 408.13 \pm 0.01\text{K}$; $P_c = 36.00 \pm 0.01\text{ atm}$; $\rho_c = 0.221 \pm 0.005\text{ g cm}^{-3}$) is based on the relation $(\partial P/\partial V)_T = 0$ at the critical point of Beattie et al. (2). The selected critical density and critical temperature, 0.221 g cm^{-3} and 408.13K , respectively, were tested with the method pro-

posed by Davis and Rice (13) together with all the experimental density data (11, 28, 31) available. Because of the unavailability of experimental density data near the critical point, the values reported by Beattie et al. (2) were accepted.

The data fit the following equation:

$$(\rho_{SL} + \rho_{SV}) = 0.4421 + 0.7414 (\rho_{SL} - \rho_{SV})^3 \quad (1)$$

Vapor Pressure

A Frost-Kalkwarf vapor-pressure equation was used with the parameters determined to fit the experimental literature values from 255K to the CP.

$$\log P = 18.54662 - 1583.23/T - 3.97829 \log T + 0.95173 (P/T^2) \quad (2)$$

where P (mm HG) and T (K).

This equation correlated the measurements of Dana et al. (11), Sage and Lacey (28), Morris et al. (25), Aston

Table I. Physical and Conversion Constants

| Constants | Value |
|-------------------------|---|
| Critical temperature | 408.13K |
| Critical pressure | 36.0 atm |
| Critical density | 0.221 g cm ⁻³ |
| Critical volume | 263.0 cm ³ mol ⁻¹ |
| Normal boiling point | 261.32K |
| Triple point | 113.55K |
| Molecular weight | 58.1243 mass units |
| Gas constant, R | 82.056060 atm cm ³ K ⁻¹ mol ⁻¹ |
| Temperature conversions | 0°C = 273.15K 0°F = 459.67°R |
| Pressure conversions | 1 atm = 760 mm Hg 1 psia = 0.06804596 atm |
| Energy conversions | 1 defined thermochemical calorie = 4.1840 J (exact) |

¹ To whom correspondence should be addressed.

Table II. Critical Constants of Isobutane

| Investigator | T_c , K | P_c , atm | ρ_c , g cm ⁻³ |
|---|-----------|-------------|-------------------------------|
| Seibert and Burrell (29), 1915 | 406.85 | 36.54 | |
| Harand (21), 1935 | 406.95 | | |
| Gilliland and Scheeline (17), 1940 | 407.61 | 37.0 | 0.249 |
| Grunberg and Nissan (18), 1948 | 407.15 | | |
| Beattie et al. (2), 1949 | 408.13 | 36.0 | 0.221 |
| Selected values, Kudchadker et al. (23), 1968 | 408.13 | 36.0 | 0.221 |
| Selected values (this work), 1973 | 408.13 | 36.0 | 0.221 |

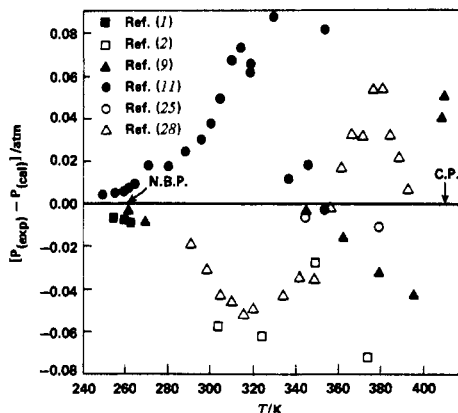


Figure 1. Isobutane vapor-pressure difference near CP

et al. (1), Wackher et al. (34), Beattie et al. (2), and Connolly (9) with an average deviation of 0.033 atm in P . In addition, the equation is also in agreement with data of Seibert and Burrell (29) and Gilliland and Scheeline (17), which were not used to determine the constants of Equation 2. At the normal boiling point of 261.32K and the critical point 408.13K, the equation agrees with the experimental values. The equation is believed to be accurate to 0.36% from 249 to CP. Figure 1 shows increased data scatter in the higher temperature range, resulting in maximum uncertainties of ± 0.1 atm. Table III, the selected saturation properties, contains the vapor pressure and its temperature derivative from the NBP to the CP.

Saturated Liquid Volume

The available measurements are those of (2, 5, 7, 8, 10, 11, 15, 16, 25, 28, 31-34) who reported their data in different temperature ranges from 224 to 398K.

For the present investigation, the data of Sliwinski (31) were selected and heavily weighted (a factor of 4) in comparison with other available literature data (2, 5, 7, 10, 11, 15, 16, 32-34). In fitting the data, the modified Guggenheim (19) equation was further modified as shown below and force fitted through the critical point. The constants of the equation were evaluated for two temperature zones meeting at a common temperature of 298.15K, and optimal fit is obtained.

$$\rho_{SL} = (\rho_L + A\theta + B\theta^2)(1.0 + \theta + 0.25\theta^3) \quad (3)$$

Table III. Saturated Properties of Isobutane

| T , K | P , atm | dP/dT | V_{SL} , cm ³ mol ⁻¹ | V_{SV} , cm ³ mol ⁻¹ | λ , cal mol ⁻¹ | H_{SL} , cal mol ⁻¹ | H_{SV} , cal mol ⁻¹ | S_{SL} , cal mol ⁻¹ K ⁻¹ | ΔS_s , cal mol ⁻¹ K ⁻¹ | S_{SV} , cal mol ⁻¹ K ⁻¹ |
|---------|-----------|---------|--|--|-----------------------------------|----------------------------------|----------------------------------|--|--|--|
| 261.32 | 1.000 | 0.0391 | 97.80 | 20682 | 5090 | 0 | 5090 | 0 | 19.478 | 19.478 |
| 270.0 | 1.390 | 0.0503 | 99.44 | 15202 | 4964 | 290 | 5254 | 0.96 | 18.385 | 19.345 |
| 280.0 | 1.968 | 0.0657 | 101.4 | 10921 | 4817 | 626 | 5443 | 2.06 | 17.204 | 19.264 |
| 290.0 | 2.714 | 0.0839 | 103.6 | 8032 | 4669 | 955 | 5624 | 3.16 | 16.100 | 19.260 |
| 300.0 | 3.656 | 0.1051 | 105.9 | 6031 | 4521 | 1288 | 5809 | 4.26 | 15.070 | 19.330 |
| 310.0 | 4.826 | 0.1293 | 108.5 | 4615 | 4372 | 1626 | 5998 | 5.39 | 14.103 | 19.493 |
| 320.0 | 6.254 | 0.1569 | 111.3 | 3577 | 4211 | 1975 | 6186 | 6.48 | 13.159 | 19.639 |
| 330.0 | 7.975 | 0.1878 | 114.5 | 2801 | 4029 | 2337 | 6366 | 7.59 | 12.209 | 19.799 |
| 340.0 | 10.02 | 0.2224 | 118.1 | 2209 | 3826 | 2719 | 6545 | 8.71 | 11.253 | 19.963 |
| 350.0 | 12.44 | 0.2608 | 122.2 | 1750 | 3596 | 3115 | 6711 | 9.84 | 10.274 | 20.114 |
| 360.0 | 15.25 | 0.3033 | 127.1 | 1387 | 3329 | 3533 | 6862 | 11.01 | 9.247 | 20.257 |
| 370.0 | 18.52 | 0.3504 | 133.1 | 1094 | 3015 | 3965 | 6980 | 12.23 | 8.149 | 20.379 |
| 380.0 | 22.28 | 0.4025 | 140.8 | 849.7 | 2624 | 4429 | 7053 | 13.56 | 6.905 | 20.465 |
| 385.0 | 24.36 | 0.4306 | 145.6 | 745.3 | 2406 | 4670 | 7076 | 14.21 | 6.249 | 20.459 |
| 390.0 | 26.59 | 0.4603 | 151.6 | 647.6 | 2155 | 4928 | 7083 | 14.89 | 5.526 | 20.416 |
| 395.0 | 28.97 | 0.4917 | 159.2 | 556.1 | 1866 | 5204 | 7070 | 15.60 | 4.724 | 20.324 |
| 396.0 | 29.46 | 0.4982 | 161.1 | 539.1 | 1805 | 5261 | 7066 | 15.74 | 4.558 | 20.298 |
| 397.0 | 29.96 | 0.5048 | 163.0 | 521.6 | 1739 | 5317 | 7056 | 15.87 | 4.380 | 20.250 |
| 398.0 | 30.47 | 0.5115 | 165.2 | 505.3 | 1676 | 5375 | 7051 | 16.01 | 4.211 | 20.221 |
| 399.0 | 30.98 | 0.5182 | 167.5 | 488.2 | 1605 | 5433 | 7038 | 16.16 | 4.023 | 20.183 |
| 400.0 | 31.51 | 0.5250 | 170.1 | 471.0 | 1529 | 5496 | 7025 | 16.31 | 3.823 | 20.133 |
| 401.0 | 32.03 | 0.5319 | 172.9 | 453.3 | 1447 | 5560 | 7007 | 16.46 | 3.608 | 20.068 |
| 402.0 | 32.57 | 0.5389 | 176.1 | 435.1 | 1358 | 5627 | 6985 | 16.62 | 3.378 | 19.998 |
| 403.0 | 33.11 | 0.5460 | 179.8 | 416.1 | 1258 | 5698 | 6956 | 16.79 | 3.122 | 19.912 |
| 404.0 | 33.66 | 0.5531 | 184.2 | 396.6 | 1149 | 5772 | 6921 | 16.97 | 2.844 | 19.814 |
| 405.0 | 34.22 | 0.5604 | 189.5 | 376.1 | 1025 | 5847 | 6872 | 17.15 | 2.531 | 19.681 |
| 406.0 | 34.78 | 0.5677 | 196.5 | 354.4 | 881 | 5933 | 6814 | 17.34 | 2.170 | 19.510 |
| 406.5 | 35.07 | 0.5715 | 201.1 | 341.8 | 791 | 5983 | 6774 | 17.45 | 1.946 | 19.396 |
| 407.0 | 35.35 | 0.5752 | 207.0 | 327.3 | 682 | 6042 | 6724 | 17.58 | 1.676 | 19.256 |
| 407.5 | 35.64 | 0.5790 | 215.4 | 309.3 | 536 | 6116 | 6652 | 17.74 | 1.315 | 19.055 |
| 408.13 | 36.00 | 0.5835 | 263.0 | 263.0 | 0 | 6443 | 6443 | 18.49 | 0 | 18.49 |

where

$\theta = [1 - (T/T_L)]^{1/3}$, T (K) and ρ (g cm^{-3}) constants of Equation 3.

| | ρ_L | A |
|-------------------|----------|-----------------------------|
| Less than 298.15K | 0.304533 | $-155.57356 \times 10^{-4}$ |
| More than 298.15K | 0.221 | 185.22760×10^{-3} |

| | B | T_L |
|-------------------|-----------------------------|--------|
| Less than 298.15K | 837.55384×10^{-4} | 393.15 |
| More than 298.15K | $-456.33640 \times 10^{-4}$ | 408.13 |

The equation represents the selected data very well over the temperature range from 224 to 398K with the standard deviation of $0.00056 \text{ g cm}^{-3}$. The values reported by Morris et al. (25), Coffin and Maass (8), and Sage and Lacey (28) are higher than the other data; hence, these sets of data were excluded in fitting the equation. Figure 2 shows how Equation 3 deviates from the experimental data. Very near the critical point, there are no data available; hence, the values accepted near the critical point are shown in Figure 3 by a solid line by use of graphical extrapolation based on rectilinear diameters and the Clapeyron equation. Selected orthobaric volumes appear in Table III.

Saturated Vapor Volume

Dana et al. (11) (273–329K), Sage and Lacey (28) (290–391K), and Sliwinski (31) (283–368K) measured the vapor volumes. At the normal boiling point, the vapor volume was calculated from the enthalpy of vaporization measurement of Aston et al. (1) via the Clapeyron equation. This value, together with other selected saturated vapor volumes (11, 31) and experimental gaseous volumes (3, 25, 28), were used to evaluate Benedict-Webb-Rubin (BWR) constants. In the evaluation of these constants, the data of Aston et al. (1) and Sliwinski (31) were weighted five times.

Figure 4 illustrates the agreement between the values (1, 28, 31). The base volumes for Figure 4 are supplied by the Equation 2 in conjunction with the BWR constants reported in Table VII. The graphically smoothed values of Figure 4 were accepted and appear in Table III.

Enthalpy of Vaporization

The enthalpies of vaporization computed from Equation 4 with Equation 2 and previously selected vapor and liquid volumes appear in Table IV in comparison of the present values to those reported by other authors (11, 12, 28). The measured enthalpy of vaporization $5089.6 \text{ cal mol}^{-1}$ of Aston et al. (1) at NBP shows close agree-

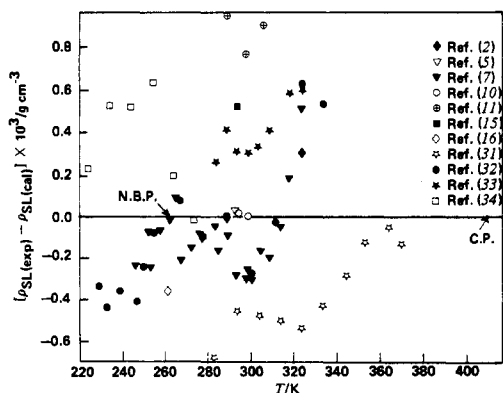


Figure 2. Isobutane saturated liquid-density difference

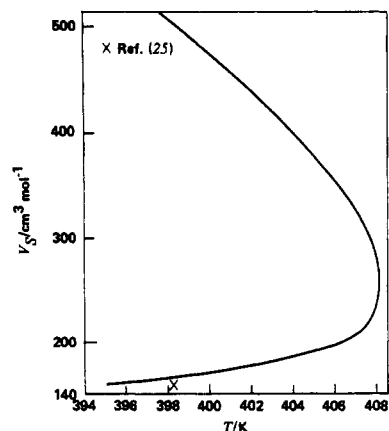


Figure 3. Saturated volume near CP

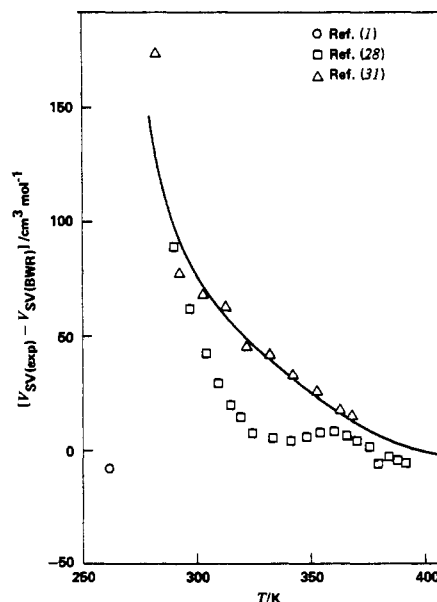


Figure 4. Saturated vapor-volume difference

Table IV. Comparison of Enthalpies of Vaporization

| T, K | λ , cal mol ⁻¹ | | | This work |
|--------|-----------------------------------|---------------------|-----------------|-----------|
| | DJBT ^{a,b} | SL ^{a,c} | DK ^d | |
| 261.32 | 5166 | | 5090 | 5090 |
| 270.0 | 4979 | | 4976 | 4964 |
| 280.0 | 4839 | | 4840 | 4817 |
| 290.0 | 4691 | (4678) ^e | 4691 | 4669 |
| 300.0 | 4534 | 4548 | 4534 | 4521 |
| 310.0 | 4358 | 4393 | 4372 | 4372 |
| 320.0 | 4160 | 4214 | 4188 | 4211 |
| 330.0 | 3952 | 4019 | 3991 | 4029 |
| 340.0 | | 3808 | 3778 | 3826 |
| 350.0 | | 3574 | 3551 | 3596 |
| 360.0 | | 3301 | 3294 | 3329 |
| 370.0 | | 2997 | 2991 | 3015 |
| 380.0 | | 2607 | 2617 | 2624 |
| 385.0 | | 2364 | | 2406 |
| 390.0 | | 2098 | 2144 | 2155 |
| 395.0 | | | | 1866 |
| 400.0 | | | 1500 | 1529 |

^a Values are interpolated. ^b Dana et al. (11). ^c Sage and Lacey (28). ^d Das and Kuloor (12). ^e Value in parentheses is extrapolated.

ment with the value 5090 cal mol⁻¹ which is calculated from the Clapeyron equation.

$$dP/dT = \lambda/[T(V_{SV} - V_{SL})] \quad (4)$$

Enthalpy of Saturated Liquid and Vapor

As no specific heat of saturated liquid data are available from the normal boiling point to the critical point, the saturated liquid enthalpy data reported by Sage and Lacey (28) have been accepted after correction to the reference state $H_{SL} = 0$ at 261.32K. A comparison of the saturated liquid enthalpies is made in Table V.

From the NBP to 390K the vapor enthalpy was obtained by addition of the enthalpy of vaporization to the liquid enthalpy calculated above. To establish the enthalpy envelope up to the critical temperature, the following graphical procedures were employed in Figure 5. Starting at 390K, the enthalpy of vaporization was marked on an overlay to Figure 5 and adjusted upward and downward until a position was obtained where both H_{SL} and H_{SV} would result in increased curvature of the envelope at the successive temperatures of Table III. As a second criterion the locus of $\bar{H} = (H_{SL} + H_{SV})/2$ was checked for smoothness. Values of H_{SL} and H_{SV} below 404K indicated that the enthalpy locus was reasonably straight. A plot of H_s vs. V_s allowed a check of the values obtained from Figure 5 in the critical region.

Entropy of Saturated Liquid and Vapor

By accepting the saturated liquid entropy data reported by Sage and Lacey (28), entropy changes along the saturated liquid envelope may be found. The values are smoothed graphically, reported in Table III, and compared in Table VI with literature data available. From NBP to 390K, the vapor entropy was obtained by addition of (λ/T) to S_{SL} . Above 390K, a graphical method identical to that for enthalpy was used with the entropy locus, $\bar{S}_s = (S_{SL} + S_{SV})/2$, reasonably straight (Figure 6) up to 405K. Again, a plot of S_s vs. V_s provided a check of entropy values at densities near the critical point.

Compressibility Data

The measurements of Sage and Lacey (28) covered 294–394K with pressures 0.68 and 204 atm. Morris et al. (25) covered a higher temperature range (311–511K) and pressure range 0.68 to 340 atm, and Beattie et al. (3) determined values over the temperature range 423–573K and pressure range 25–304 atm. The data reported by Beattie et al. (3) are in good agreement with those of Morris et al. (25). Figure 7 shows the P,T regions of these major data sources.

Correlation Procedure

Although agreement between the major data sources is not good in some regions, no sound reason was found for deletion of any point, and each point was given equal weight. Saturated vapor volumes selected in Table III were added to the present PVT data sets and given a weight of five, except for the critical point and boiling point which were weighted ten. This procedure was used to constrain the PVT surface to values consistent with the selected saturated properties which form a boundary condition. The differential regional BWR equation (14) is

$$\varphi = \sum_{r=1}^N \sum_{j=1}^7 K_{jr} \cdot \theta_j^* \quad (5)$$

Table V. Comparison of Saturated Liquid Enthalpies

| T, K | H_{SL} , cal mol ⁻¹ | | | |
|--------|----------------------------------|--------------------|-----------------|-----------|
| | DJBT ^{a,b} | SL ^{a,c} | DK ^d | This work |
| 261.32 | 0 | (0) ^e | 0 | 0 |
| 270.0 | 318 | (290) ^e | 267 | 290 |
| 280.0 | 635 | (626) ^e | 587 | 626 |
| 290.0 | 990 | (955) ^e | 920 | 955 |
| 300.0 | 1385 | 1288 | 1258 | 1288 |
| 310.0 | 1809 | 1626 | 1604 | 1626 |
| 320.0 | 2273 | 1975 | 1967 | 1975 |
| 330.0 | 2774 | 2337 | 2340 | 2337 |
| 340.0 | | 2719 | 2725 | 2719 |
| 350.0 | | 3115 | 3115 | 3115 |
| 360.0 | | 3533 | 3527 | 3533 |
| 370.0 | | 3965 | 3966 | 3965 |
| 380.0 | | 4429 | 4445 | 4429 |
| 385.0 | | 4657 | | 4670 |
| 390.0 | | 4923 | 4969 | 4928 |
| 395.0 | | | | 5204 |
| 400.0 | | | 5570 | 5496 |

^a Values are interpolated. ^b Dana et al. (11). ^c Sage and Lacey (28). ^d Das and Kuloor (12). ^e Values in parentheses are extrapolated.

Table VI. Comparison of Saturated Liquid Entropies

| T, K | S_{SL} , cal K ⁻¹ mol ⁻¹ | | | |
|--------|--|-------------------|-----------------|-----------|
| | DJBT ^{a,b} | SL ^{a,c} | DK ^d | This work |
| 261.32 | 0 | 0 | 0 | 0 |
| 270.0 | 1.02 | 0.96 | 1.03 | 0.96 |
| 280.0 | 2.18 | 2.06 | 2.18 | 2.06 |
| 290.0 | 3.40 | 3.16 | 3.36 | 3.16 |
| 300.0 | 4.74 | 4.26 | 4.49 | 4.26 |
| 310.0 | 6.12 | 5.39 | 5.62 | 5.39 |
| 320.0 | 7.56 | 6.48 | 6.74 | 6.48 |
| 330.0 | 9.13 | 7.59 | 7.87 | 7.59 |
| 340.0 | | 8.71 | 8.99 | 8.71 |
| 350.0 | | 9.84 | 10.10 | 9.84 |
| 360.0 | | 11.01 | 11.23 | 11.01 |
| 370.0 | | 12.23 | 12.41 | 12.23 |
| 380.0 | | 13.56 | 13.64 | 13.56 |
| 385.0 | | 14.21 | | 14.21 |
| 390.0 | | 14.82 | 14.87 | 14.89 |
| 395.0 | | | | 15.60 |
| 400.0 | | | 16.45 | 16.31 |

^a Values are interpolated. ^b Dana et al. (11). ^c Sage and Lacey (28). ^d Das and Kuloor (12).

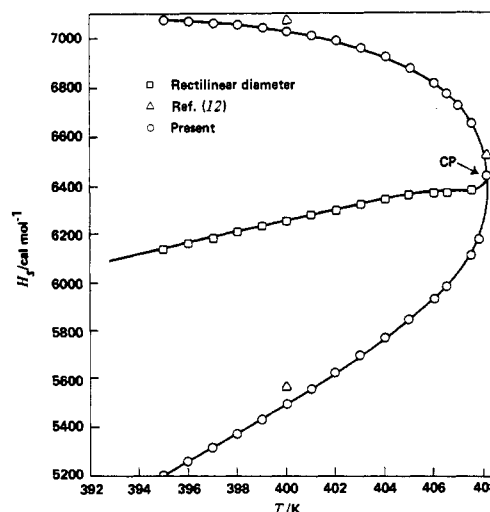


Figure 5. Enthalpy envelope

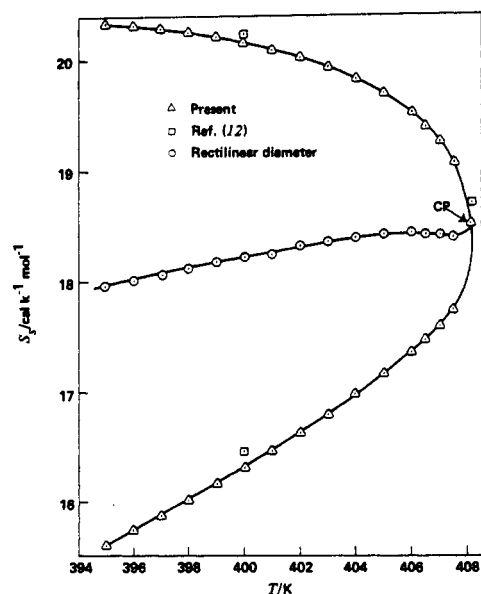


Figure 6. Entropy envelope

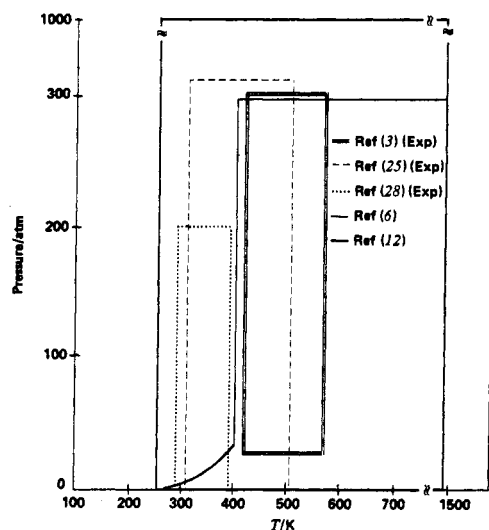


Figure 7. Regional block diagram of literature data for isobutane

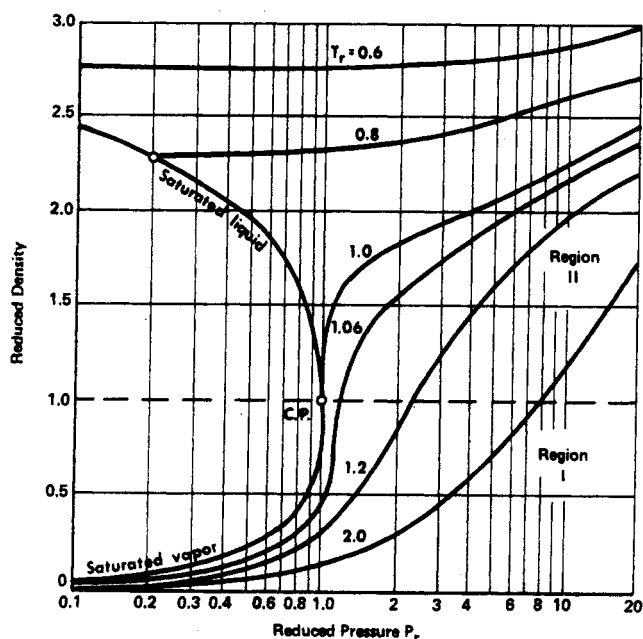


Figure 8. Isobutane gas PVT regions

where

$$\varphi = P - RT\rho, \theta_1^* = RT(\rho^*)^2, \theta_2^* = (\rho^*)^2$$

$$\theta_3^* = (\rho^*)^2 T^{-2}, \theta_4^* = RT(\rho^*)^3, \theta_5^* = (\rho^*)^3$$

$$\theta_6^* = (\rho^*)^6, \theta_7^* = (\rho^*)^3 [1 + K_{8r}(\rho^*)^2] [\exp(-K_{8r}\rho^*)] T^{-2}$$

$$\rho^* = \rho - \rho_{r-1}, n_{r-1}$$

with ρ_{r-1}, n_{r-1} equal to the density at the interface between regions r and $r-1$ when the density ρ falls in region r . An optimal fit is generally obtained when the interface between the first and second regions is equal to the critical density. For isobutane there were not sufficient data at densities above the critical point to require more than one region to provide an optimal fit as shown by Figure 8. Standard BWR coefficients for the first region ($K_{11} = B_0, K_{21} = -A_0, K_{31} = -C_0, K_{41} = b, K_{51} = -a, K_{61} = a\alpha, K_{71} = c, \text{ and } K_{81} = +\gamma$) and coefficients of Equation 5 for the first and second regions are found in Table VII. The latter coefficients are used only with normalized densities. Table VII also provides the first region constants in the usual metric units for comparison to literature BWR coefficients.

Accuracy of Saturated Properties

The selected liquid volumes of Table III are considered accurate to a maximum of $\pm 0.2\%$ from NBP to 320K and maximum of 0.5% from 320 to 370K. The error limit of vapor volume at NBP is $14 \text{ cm}^3 \text{ mol}^{-1}$, providing the measurement of enthalpy of vaporization of Aston and Kennedy (7) is correct. Figure 4 indicates the uncertainty with respect to the equation of state in the vapor volume. The accuracy of enthalpy of vaporization values in Table III depends on that of vapor-pressure slope and vapor volume with error limits of 1.0% for dP/dT . The uncer-

Table VII. Constants for the DR-BWR Equation

| | Region I | Region II |
|---------------------------------------|--------------------------|---------------------------|
| Number of data points | 308 | 75 |
| Density range, g mol cm^{-3} | 0.0 to 0.0038022 | 0.0038022 to 0.008710174 |
| Normalized density range | 0.00244 to 0.4365 | 0.4365 to 1 |
| Av % deviation for Z | 0.4731 | 0.3205 |
| Max % deviation for Z | 0.6787 | 1.3260 |
| Constants for Equation 1 ^a | | |
| K_{1r} | 6.06741×10^{-3} | 2.56545×10^{-2} |
| K_{2r} | -5.07260×10^2 | -8.55723×10^2 |
| K_{3r} | -8.64777×10^7 | -1.06304×10^7 |
| K_{4r} | 3.00792×10^{-2} | -5.99536×10^{-2} |
| K_{5r} | -1.45155×10^3 | 4.53234×10^3 |
| K_{6r} | 4.89167×10^2 | -1.57375×10^3 |
| K_{7r} | 2.10348×10^8 | -2.62513×10^8 |
| K_{8r} | 2.00000 | 8.00000 |
| BWR constants ^b | | |
| A_0 | 6.68616×10^6 | |
| B_0 | 7.99741×10 | |
| C_0 | 1.13986×10^{12} | |
| a | 2.19660×10^9 | |
| b | 4.55183×10^4 | |
| c | 3.18315×10^{14} | |
| α | 5.09970×10^6 | |
| γ | 2.63619×10^4 | |

^a Only for use in Equation 5 with ρ normalized as $(\text{g mol cm}^{-3} / 0.008710174)$. ^b $P - RT\rho = (B_0RT - A_0 - C_0/T^2)\rho^2 + (bRT - a)\rho^3 + a\alpha\rho^6 + (c\rho^3/T^2)[1 + \gamma\rho^2]e^{-\gamma\rho^2}$; P (atm), T (K), ρ (g mol cm^{-3}).

tainty is ± 40 cal mol⁻¹ from NBP to 385K. Above 385K, the prime source of error is dP/dT rather than the vapor volume or liquid volume. The liquid enthalpies of Table III are judged accurate 0.3% as reported by Sage and Lacey (28) except near the critical point. The H_s vs. V_s and S_s vs. V_s diagrams were drawn to check these extrapolated values from 390K to CP. Liquid entropy values are likewise considered accurate within $\pm 0.3\%$ from NBP to 385K.

PVT Surface and Corresponding Thermodynamic Properties

Table VII shows the ability of the DR-BWR model to fit the available experimental PVT data. Both experimental data and isotherms from the model were plotted as compressibility factor $Z = (P/\rho RT)$ vs. pressure on large graphs such that the finest division was 0.0005 for Z . The Z - P graphs show that in all regions, the model provides a smooth surface with reasonable compromise between the experimental results.

Thermodynamic properties were calculated from the PVT surface by the usual relationships and appear in Table VIII, a condensed version of the API Research Project 44 j-tables (a complete version of Table VIII has

been deposited in the ACS Microfilm Depository Service). Values of pressure in parentheses are at saturated conditions. The tables are thermodynamically consistent as the other functions were calculated from $A - A^\circ$ and $S - S^\circ$ where A is the energy function for density and temperature with S its temperature derivative. Table VIII extends only to 600K or slightly above the maximum experimental temperature of 573K rather than 1500K as in the revised API Research Project 44 tables. The values above 573K are an extrapolation of the present surface and further assume no decomposition of the isobutane.

Discussion

Table IX is a comparison of these values with values calculated from corresponding states by two methods: the corresponding state tables of Lydersen et al. (24) and Pitzer's (26, 27) acentric factor procedure.

Table X is a comparison of the selected second virial coefficients of Jessen and Lightfoot (22), Connolly (9), Gunn (20), and API (h-tables) (30) with the present value where

$$B = B_0 - \frac{A_0}{RT} - \frac{C_0}{RT^3} \quad (6)$$

Table VIII (Condensed). Thermodynamic Properties of Isobutane

| Press, atm | Z | $H - H^\circ$, cal mol ⁻¹ | $(H - H^\circ)/T$, cal mol ⁻¹ K ⁻¹ | $A - A^\circ$, cal mol ⁻¹ | $S - S^\circ$, cal mol ⁻¹ K ⁻¹ | $S - S^I$, cal mol ⁻¹ | $G - G^\circ$, cal mol ⁻¹ | $(G - G^\circ)/T$, cal mol ⁻¹ K ⁻¹ | $G - G^I$, cal mol ⁻¹ | (f/p) |
|--------------------|--------|--|---|--|--|--------------------------------------|--|---|--------------------------------------|--------|
| 270K | | | | | | | | | | |
| 1 | 0.9566 | -84.203 | -0.312 | 0.434 | -0.2272 | -0.2272 | -22.9 | -0.085 | -22.9 | 0.9583 |
| 1.390 ^a | 0.9386 | -119.030 | -0.441 | 177.560 | -0.9766 | -0.3222 | 144.7 | 0.536 | -32.0 | 0.9420 |
| 280K | | | | | | | | | | |
| 1 | 0.9621 | -75.908 | -0.271 | 0.337 | -0.1970 | -0.1970 | -20.7 | -0.074 | -20.7 | 0.9634 |
| 1.968 ^a | 0.9228 | -154.922 | -0.553 | 377.931 | -1.7497 | -0.4051 | 335.0 | 1.196 | -41.5 | 0.9281 |
| 300K | | | | | | | | | | |
| 1 | 0.9706 | -62.579 | -0.209 | 0.210 | -0.1510 | -0.1510 | -17.3 | -0.058 | -17.3 | 0.9714 |
| 3.656 ^a | 0.8842 | -247.756 | -0.826 | 775.859 | -3.1821 | -0.6075 | 706.9 | 2.356 | -65.5 | 0.8959 |
| 320K | | | | | | | | | | |
| 1 | 0.9768 | -52.441 | -0.164 | 0.135 | -0.1182 | -0.1182 | -14.6 | -0.046 | -14.6 | 0.9773 |
| 4 | 0.9011 | -224.364 | -0.701 | 883.549 | -3.2658 | -0.5129 | 820.7 | 2.565 | -60.2 | 0.9095 |
| 6.254 ^a | 0.8360 | -373.601 | -1.168 | 1172.517 | -4.5059 | -0.8653 | 1068.3 | 3.338 | -96.7 | 0.8589 |
| 340K | | | | | | | | | | |
| 1 | 0.9813 | -44.555 | -0.131 | 0.089 | -0.0943 | -0.0943 | -12.5 | -0.037 | -12.5 | 0.9816 |
| 4 | 0.9218 | -187.562 | -0.552 | 937.653 | -3.1541 | -0.4011 | 884.8 | 2.602 | -51.2 | 0.9270 |
| 8 | 0.8307 | -408.562 | -1.202 | 1412.309 | -5.0193 | -0.8898 | 1298.0 | 3.818 | -106.0 | 0.8547 |
| 10.02 ^a | 0.7767 | -541.078 | -1.591 | 1571.343 | -5.7695 | -1.1924 | 1420.6 | 4.178 | -135.7 | 0.8180 |
| 360K | | | | | | | | | | |
| 1 | 0.9848 | -38.306 | -0.106 | 0.060 | -0.0764 | -0.0764 | -10.8 | -0.030 | -10.8 | 0.9850 |
| 4 | 0.9370 | -159.433 | -0.443 | 992.142 | -3.0736 | -0.3207 | 947.1 | 2.631 | -44.0 | 0.9403 |
| 8 | 0.8665 | -339.473 | -0.943 | 1491.705 | -4.8215 | -0.6921 | 1396.3 | 3.879 | -90.3 | 0.8813 |
| 12 | 0.7846 | -551.570 | -1.532 | 1790.691 | -6.0786 | -1.1440 | 1636.7 | 4.546 | -139.7 | 0.8224 |
| 15.25 ^a | 0.7032 | -766.171 | -2.128 | 1977.030 | -7.0306 | -1.6196 | 1764.8 | 4.902 | -183.1 | 0.7740 |
| 380K | | | | | | | | | | |
| 1 | 0.9875 | -33.276 | -0.088 | 0.042 | -0.0628 | -0.0628 | -9.4 | -0.025 | -9.4 | 0.9876 |
| 4 | 0.9484 | -137.358 | -0.361 | 1046.849 | -3.0139 | -0.2609 | 1007.9 | 2.652 | -38.2 | 0.9506 |
| 8 | 0.8923 | -288.124 | -0.758 | 1572.471 | -4.6825 | -0.5531 | 1491.2 | 3.924 | -78.0 | 0.9019 |
| 12 | 0.8301 | -457.394 | -1.204 | 1883.750 | -5.8236 | -0.8890 | 1755.6 | 4.620 | -119.6 | 0.8534 |
| 16 | 0.7588 | -654.528 | -1.722 | 2110.622 | -6.7978 | -1.2918 | 1928.6 | 5.075 | -163.6 | 0.8051 |
| 20 | 0.6715 | -901.051 | -2.371 | 2297.492 | -7.7650 | -1.8159 | 2049.6 | 5.394 | -211.0 | 0.7561 |
| 22.28 ^a | 0.6074 | -1086.721 | -2.860 | 2398.073 | -8.3909 | -2.2277 | 2101.8 | 5.531 | -240.2 | 0.7274 |
| 390K | | | | | | | | | | |
| 1 | 0.9886 | -31.121 | -0.080 | 0.035 | -0.0572 | -0.0572 | -8.8 | -0.023 | -8.8 | 0.9887 |
| 4 | 0.9531 | -128.044 | -0.328 | 1074.252 | -2.9897 | -0.2367 | 1037.9 | 2.661 | -35.7 | 0.9549 |
| 8 | 0.9027 | -267.076 | -0.685 | 1613.149 | -4.6278 | -0.4984 | 1537.8 | 3.943 | -72.7 | 0.9104 |
| 12 | 0.8476 | -420.620 | -1.079 | 1931.321 | -5.7280 | -0.7934 | 1813.3 | 4.650 | -111.2 | 0.8663 |
| 16 | 0.7862 | -594.575 | -1.525 | 2161.410 | -6.6420 | -1.1360 | 1995.8 | 5.117 | -151.5 | 0.8223 |

Table VIII (Condensed). Continued

| Press, atm | Z | $H - H^0$, cal mol ⁻¹ | $(H - H^0)/T$, cal mol ⁻¹ K ⁻¹ | $A - A^0$, cal mol ⁻¹ | $S - S^0$, cal mol ⁻¹ K ⁻¹ | $S - S^f$, cal mol ⁻¹ | $G - G^0$, cal mol ⁻¹ | $(G - G^0)/T$, cal mol ⁻¹ K ⁻¹ | $G - G^f$, cal mol ⁻¹ | (f/p) |
|--------------------|--------|--------------------------------------|---|--------------------------------------|--|--------------------------------------|--------------------------------------|---|--------------------------------------|--------|
| 390K | | | | | | | | | | |
| 20 | 0.7148 | -800.250 | -2.052 | 2346.752 | -7.5030 | -1.5539 | 2125.9 | 5.451 | -194.2 | 0.7782 |
| 24 | 0.6253 | -1065.782 | -2.733 | 2511.211 | -8.4277 | -2.1166 | 2221.0 | 5.695 | -240.3 | 0.7332 |
| 26.59 ^a | 0.5441 | -1315.783 | -3.374 | 2620.701 | -9.1883 | -2.6739 | 2267.6 | 5.814 | -273.0 | 0.7030 |
| 400K | | | | | | | | | | |
| 1 | 0.9895 | -29.169 | -0.073 | 0.029 | -0.0522 | -0.0522 | -8.3 | -0.021 | -8.3 | 0.9896 |
| 4 | 0.9573 | -119.667 | -0.299 | 1101.679 | -2.9685 | -0.2155 | 1067.7 | 2.669 | -33.5 | 0.9587 |
| 8 | 0.9117 | -248.417 | -0.621 | 1653.955 | -4.5806 | -0.4511 | 1583.8 | 3.960 | -68.0 | 0.9180 |
| 12 | 0.8626 | -388.737 | -0.972 | 1979.317 | -5.6473 | -0.7127 | 1870.2 | 4.675 | -103.7 | 0.8776 |
| 16 | 0.8089 | -544.476 | -1.361 | 2213.381 | -6.5151 | -1.0092 | 2061.6 | 5.154 | -140.8 | 0.8376 |
| 20 | 0.7486 | -722.193 | -1.805 | 2399.607 | -7.3052 | -1.3562 | 2199.9 | 5.500 | -179.7 | 0.7975 |
| 24 | 0.6782 | -934.762 | -2.337 | 2559.183 | -8.0957 | -1.7846 | 2303.5 | 5.759 | -220.9 | 0.7572 |
| 28 | 0.5883 | -1215.698 | -3.039 | 2708.504 | -8.9930 | -2.3758 | 2381.5 | 5.954 | -265.4 | 0.7160 |
| 29 | 0.5599 | -1307.625 | -3.269 | 2747.122 | -9.2628 | -2.5759 | 2397.5 | 5.994 | -277.3 | 0.7054 |
| 30 | 0.5267 | -1417.134 | -3.543 | 2788.151 | -9.5732 | -2.8190 | 2412.2 | 6.030 | -289.5 | 0.6945 |
| 31 | 0.4847 | -1559.408 | -3.899 | 2834.661 | -9.9619 | -3.1426 | 2425.4 | 6.063 | -302.4 | 0.6834 |
| 31.51 ^a | 0.4564 | -1658.466 | -4.146 | 2863.209 | -10.2248 | -3.3732 | 2431.4 | 6.079 | -309.2 | 0.6776 |
| 406K | | | | | | | | | | |
| 1 | 0.9901 | -28.084 | -0.069 | 0.026 | -0.0495 | -0.0495 | -8.0 | -0.020 | -8.0 | 0.9902 |
| 4 | 0.9595 | -115.038 | -0.283 | 1118.145 | -2.9570 | -0.2040 | 1085.5 | 2.674 | -32.2 | 0.9608 |
| 8 | 0.9166 | -238.208 | -0.587 | 1678.486 | -4.5552 | -0.4258 | 1611.2 | 3.969 | -65.3 | 0.9222 |
| 12 | 0.8706 | -371.544 | -0.915 | 2008.264 | -5.6046 | -0.6700 | 1903.9 | 4.689 | -99.5 | 0.8839 |
| 16 | 0.8208 | -518.072 | -1.276 | 2244.961 | -6.4496 | -0.9436 | 2100.4 | 5.174 | -135.0 | 0.8459 |
| 20 | 0.7657 | -682.647 | -1.681 | 2432.339 | -7.2071 | -1.2580 | 2243.4 | 5.526 | -171.9 | 0.8080 |
| 24 | 0.7030 | -873.988 | -2.153 | 2591.060 | -7.9449 | -1.6338 | 2351.6 | 5.792 | -210.7 | 0.7700 |
| 28 | 0.6279 | -1110.756 | -2.736 | 2734.679 | -8.7325 | -2.1153 | 2434.6 | 5.997 | -252.0 | 0.7316 |
| 29 | 0.6059 | -1181.774 | -2.911 | 2769.860 | -8.9504 | -2.2635 | 2452.1 | 6.040 | -262.8 | 0.7218 |
| 30 | 0.5819 | -1260.187 | -3.104 | 2805.395 | -9.1836 | -2.4293 | 2468.3 | 6.080 | -273.9 | 0.7120 |
| 31 | 0.5554 | -1348.656 | -3.322 | 2841.841 | -9.4385 | -2.6191 | 2483.4 | 6.117 | -285.3 | 0.7020 |
| 32 | 0.5251 | -1451.843 | -3.576 | 2880.115 | -9.7268 | -2.8443 | 2497.2 | 6.151 | -297.0 | 0.6918 |
| 33 | 0.4887 | -1579.418 | -3.890 | 2922.058 | -10.0720 | -3.1285 | 2509.8 | 6.182 | -309.3 | 0.6814 |
| 34 | 0.4397 | -1758.918 | -4.332 | 2972.756 | -10.5417 | -3.5389 | 2521.0 | 6.209 | -322.1 | 0.6706 |
| 34.78 ^a | 0.3657 | -2054.975 | -5.062 | 3039.961 | -11.2895 | -4.2414 | 2528.6 | 6.228 | -333.0 | 0.6617 |
| 408K | | | | | | | | | | |
| 1 | 0.9903 | -27.735 | -0.068 | 0.025 | -0.0487 | -0.0487 | -7.9 | -0.019 | -7.9 | 0.9903 |
| 4 | 0.9602 | -113.556 | -0.278 | 1123.635 | -2.9533 | -0.2004 | 1091.4 | 2.675 | -31.8 | 0.9615 |
| 8 | 0.9181 | -234.953 | -0.576 | 1686.670 | -4.5472 | -0.4178 | 1620.3 | 3.971 | -64.5 | 0.9235 |
| 12 | 0.8731 | -366.098 | -0.897 | 2017.933 | -5.5913 | -0.6566 | 1915.1 | 4.694 | -98.2 | 0.8859 |
| 16 | 0.8245 | -509.788 | -1.249 | 2255.540 | -6.4292 | -0.9233 | 2113.3 | 5.180 | -133.1 | 0.8485 |
| 20 | 0.7710 | -670.436 | -1.643 | 2443.378 | -7.1771 | -1.2280 | 2257.8 | 5.534 | -169.4 | 0.8113 |
| 24 | 0.7105 | -855.754 | -2.097 | 2602.009 | -7.9001 | -1.5890 | 2367.5 | 5.803 | -207.5 | 0.7741 |
| 28 | 0.6391 | -1081.465 | -2.651 | 2744.462 | -8.6605 | -2.0433 | 2452.0 | 6.010 | -247.8 | 0.7365 |
| 29 | 0.6185 | -1147.950 | -2.814 | 2778.995 | -8.8673 | -2.1804 | 2469.9 | 6.054 | -258.4 | 0.7270 |
| 30 | 0.5964 | -1220.420 | -2.991 | 2813.603 | -9.0858 | -2.3316 | 2486.6 | 6.095 | -269.1 | 0.7174 |
| 31 | 0.5723 | -1300.667 | -3.188 | 2848.674 | -9.3206 | -2.5012 | 2502.1 | 6.133 | -280.2 | 0.7077 |
| 32 | 0.5455 | -1391.544 | -3.411 | 2884.782 | -9.5786 | -2.6962 | 2516.5 | 6.168 | -291.5 | 0.6978 |
| 33 | 0.5148 | -1498.084 | -3.672 | 2922.883 | -9.8721 | -2.9286 | 2529.7 | 6.200 | -303.2 | 0.6878 |
| 34 | 0.4778 | -1630.802 | -3.997 | 2964.908 | -10.2269 | -3.2241 | 2541.8 | 6.230 | -315.4 | 0.6776 |
| 35 | 0.4277 | -1819.730 | -4.460 | 3016.172 | -10.7161 | -3.6558 | 2552.4 | 6.256 | -328.2 | 0.6669 |
| 35.93 ^a | 0.3069 | -2352.159 | -5.765 | 3122.311 | -12.0413 | -4.9287 | 2560.7 | 6.276 | -341.3 | 0.6563 |
| 410K | | | | | | | | | | |
| 1 | 0.9904 | -27.393 | -0.067 | 0.024 | -0.0478 | -0.0478 | -7.8 | -0.019 | -7.8 | 0.9905 |
| 20 | 0.7761 | -658.655 | -1.606 | 2454.471 | -7.1483 | -1.1992 | 2272.1 | 5.542 | -167.0 | 0.8146 |
| 30 | 0.6096 | -1184.495 | -2.889 | 2822.533 | -8.9980 | -2.2438 | 2504.7 | 6.109 | -264.6 | 0.7226 |
| 40 | 0.2148 | -3118.417 | -7.606 | 3245.775 | -13.9631 | -6.6376 | 2606.5 | 6.357 | -397.0 | 0.6141 |
| 52 | 0.2430 | -3389.541 | -8.267 | 3270.990 | -14.7419 | -6.8953 | 2654.6 | 6.475 | -562.5 | 0.5012 |
| 60 | 0.2695 | -3464.068 | -8.449 | 3279.157 | -14.9963 | -6.8656 | 2684.4 | 6.547 | -649.2 | 0.4505 |
| 72 | 0.3109 | -3534.330 | -8.620 | 3288.496 | -15.2725 | -6.7797 | 2727.4 | 6.652 | -754.6 | 0.3958 |
| 80 | 0.3386 | -3566.620 | -8.699 | 3293.766 | -15.4192 | -6.7171 | 2755.2 | 6.720 | -812.6 | 0.3686 |
| 100 | 0.4074 | -3620.148 | -8.830 | 3305.273 | -15.7145 | -6.5693 | 2822.8 | 6.885 | -926.7 | 0.3204 |
| 120 | 0.4751 | -3651.131 | -8.905 | 3315.480 | -15.9495 | -6.4423 | 2888.1 | 7.044 | -1009.8 | 0.2893 |
| 140 | 0.5417 | -3668.974 | -8.949 | 3324.982 | -16.1484 | -6.3351 | 2951.9 | 7.200 | -1071.6 | 0.2682 |
| 160 | 0.6072 | -3678.176 | -8.971 | 3334.052 | -16.3230 | -6.2445 | 3014.3 | 7.352 | -1117.9 | 0.2533 |
| 180 | 0.6717 | -3681.243 | -8.979 | 3342.834 | -16.4799 | -6.1675 | 3075.5 | 7.501 | -1152.6 | 0.2428 |
| 200 | 0.7352 | -3679.729 | -8.975 | 3351.413 | -16.6233 | -6.1017 | 3135.8 | 7.648 | -1178.0 | 0.2353 |

(Continued on page 260)

Table VIII (Condensed). Continued

| Press, atm | z | $H - H^{\circ}$, cal mol ⁻¹ | $(H - H^{\circ})/T$, cal mol ⁻¹ K ⁻¹ | $A - A^{\circ}$, cal mol ⁻¹ | $s - s^{\circ}$, cal mol ⁻¹ K ⁻¹ | $s - s^I$, cal mol ⁻¹ | $G - G^{\circ}$, cal mol ⁻¹ | $(G - G^{\circ})/T$, cal mol ⁻¹ K ⁻¹ | $G - G^I$, cal mol ⁻¹ | (f/p) |
|---------------|--------|--|---|--|---|--------------------------------------|--|---|--------------------------------------|--------|
| 410K | | | | | | | | | | |
| 220 | 0.7979 | -3674.665 | -8.963 | 3359.845 | -16.7560 | -6.0451 | 3195.3 | 7.793 | -1196.2 | 0.2301 |
| 240 | 0.8597 | -3666.773 | -8.943 | 3368.167 | -16.8799 | -5.9962 | 3254.0 | 7.937 | -1208.3 | 0.2267 |
| 260 | 0.9209 | -3656.576 | -8.918 | 3376.405 | -16.9964 | -5.9538 | 3312.0 | 8.078 | -1215.5 | 0.2247 |
| 280 | 0.9813 | -3644.467 | -8.889 | 3384.578 | -17.1068 | -5.9170 | 3369.3 | 8.218 | -1218.5 | 0.2239 |
| 300 | 1.0410 | -3630.748 | -8.855 | 3392.700 | -17.2119 | -5.8851 | 3426.1 | 8.356 | -1217.9 | 0.2241 |
| 350 | 1.1879 | -3590.852 | -8.758 | 3412.846 | -17.4552 | -5.8223 | 3565.8 | 8.697 | -1203.7 | 0.2280 |
| 400 | 1.3313 | -3544.889 | -8.646 | 3432.842 | -17.6768 | -5.7787 | 3702.6 | 9.031 | -1175.6 | 0.2360 |
| 440K | | | | | | | | | | |
| 1 | 0.9925 | -22.939 | -0.052 | 0.014 | -0.0373 | -0.0373 | -6.5 | -0.015 | -6.5 | 0.9926 |
| 20 | 0.8354 | -520.024 | -1.182 | 2625.099 | -6.8211 | -0.8721 | 2481.3 | 5.639 | -136.3 | 0.8556 |
| 40 | 0.6147 | -1291.334 | -2.935 | 3268.845 | -9.5989 | -2.2733 | 2932.2 | 6.664 | -291.1 | 0.7167 |
| 60 | 0.3749 | -2540.856 | -5.775 | 3650.868 | -12.8307 | -4.7000 | 3104.6 | 7.056 | -472.9 | 0.5821 |
| 80 | 0.3859 | -2984.909 | -6.784 | 3734.690 | -14.0523 | -5.3503 | 3198.1 | 7.268 | -630.8 | 0.4858 |
| 100 | 0.4381 | -3153.223 | -7.166 | 3769.016 | -14.6165 | -5.4713 | 3278.0 | 7.450 | -745.8 | 0.4259 |
| 120 | 0.4968 | -3243.431 | -7.371 | 3792.005 | -14.9903 | -5.4831 | 3352.3 | 7.619 | -830.9 | 0.3864 |
| 140 | 0.5570 | -3297.793 | -7.495 | 3810.239 | -15.2749 | -5.4616 | 3423.2 | 7.780 | -894.7 | 0.3592 |
| 160 | 0.6174 | -3331.904 | -7.573 | 3825.927 | -15.5080 | -5.4295 | 3491.6 | 7.935 | -942.9 | 0.3399 |
| 180 | 0.6774 | -3353.088 | -7.621 | 3840.047 | -15.7074 | -5.3950 | 3558.2 | 8.087 | -979.3 | 0.3260 |
| 200 | 0.7369 | -3365.347 | -7.649 | 3853.115 | -15.8832 | -5.3615 | 3623.2 | 8.235 | -1006.3 | 0.3161 |
| 220 | 0.7958 | -3371.083 | -7.662 | 3865.431 | -16.0412 | -5.3303 | 3687.0 | 8.380 | -1025.8 | 0.3091 |
| 240 | 0.8541 | -3371.860 | -7.663 | 3877.185 | -16.1854 | -5.3017 | 3749.7 | 8.522 | -1039.1 | 0.3045 |
| 260 | 0.9118 | -3368.745 | -7.656 | 3888.505 | -16.3186 | -5.2760 | 3811.5 | 8.662 | -1047.3 | 0.3016 |
| 280 | 0.9689 | -3362.501 | -7.642 | 3899.482 | -16.4428 | -5.2530 | 3872.3 | 8.801 | -1051.2 | 0.3003 |
| 300 | 1.0255 | -3353.692 | -7.622 | 3910.181 | -16.5594 | -5.2325 | 3932.4 | 8.937 | -1051.4 | 0.3002 |
| 350 | 1.1645 | -3323.021 | -7.552 | 3936.004 | -16.8244 | -5.1914 | 4079.7 | 9.272 | -1038.8 | 0.3046 |
| 400 | 1.3004 | -3283.281 | -7.462 | 3960.875 | -17.0605 | -5.1624 | 4223.3 | 9.599 | -1011.8 | 0.4141 |
| 520K | | | | | | | | | | |
| 1 | 0.9959 | -15.254 | -0.029 | 0.003 | -0.0212 | -0.0212 | -4.3 | -0.008 | -4.3 | 0.9959 |
| 20 | 0.9158 | -322.133 | -0.619 | 3094.459 | -6.4032 | -0.4542 | 3007.5 | 5.784 | -86.0 | 0.9201 |
| 40 | 0.8293 | -684.590 | -1.317 | 3812.006 | -8.3082 | -0.9827 | 3635.7 | 6.992 | -173.6 | 0.8453 |
| 60 | 0.7463 | -1086.281 | -2.089 | 4228.365 | -9.7166 | -1.5859 | 3966.4 | 7.628 | -261.6 | 0.7762 |
| 80 | 0.6813 | -1495.496 | -2.876 | 4507.363 | -10.9110 | -2.2090 | 4178.2 | 8.035 | -346.8 | 0.7147 |
| 100 | 0.6471 | -1852.951 | -3.563 | 4695.186 | -11.8918 | -2.7467 | 4330.8 | 8.328 | -424.7 | 0.6628 |
| 120 | 0.6455 | -2116.811 | -4.071 | 4818.002 | -12.6322 | -3.1250 | 4451.9 | 8.561 | -491.8 | 0.6211 |
| 140 | 0.6700 | -2284.958 | -4.394 | 4897.123 | -13.1564 | -3.3430 | 4556.4 | 8.762 | -546.6 | 0.5890 |
| 160 | 0.7057 | -2400.335 | -4.616 | 4954.952 | -13.5604 | -3.4819 | 4651.1 | 8.944 | -589.8 | 0.5649 |
| 180 | 0.7466 | -2483.889 | -4.777 | 5000.931 | -13.8908 | -3.5784 | 4739.3 | 9.114 | -623.1 | 0.5469 |
| 200 | 0.7903 | -2545.934 | -4.896 | 5039.401 | -14.1707 | -3.6491 | 4822.9 | 9.275 | -648.4 | 0.5337 |
| 220 | 0.8355 | -2592.364 | -4.985 | 5072.699 | -14.4138 | -3.7029 | 4902.8 | 9.428 | -666.9 | 0.5243 |
| 240 | 0.8816 | -2626.925 | -5.052 | 5102.228 | -14.6285 | -3.7449 | 4979.9 | 9.577 | -679.6 | 0.5178 |
| 260 | 0.9281 | -2652.210 | -5.100 | 5128.906 | -14.8209 | -3.7783 | 5054.7 | 9.721 | -687.5 | 0.5139 |
| 280 | 0.9749 | -2670.092 | -5.135 | 5153.366 | -14.9953 | -3.8055 | 5127.5 | 9.861 | -691.2 | 0.5120 |
| 300 | 1.0218 | -2681.966 | -5.158 | 5176.060 | -15.1549 | -3.8281 | 5198.6 | 9.997 | -691.4 | 0.5120 |
| 350 | 1.1387 | -2691.764 | -5.176 | 5227.060 | -15.5040 | -3.8711 | 5370.3 | 10.328 | -678.8 | 0.5182 |
| 400 | 1.2546 | -2681.233 | -5.156 | 5272.285 | -15.8008 | -3.9026 | 5535.2 | 10.645 | -651.9 | 0.5319 |
| 600K | | | | | | | | | | |
| 1 | 0.9976 | -10.872 | -0.018 | -0.008 | -0.0133 | -0.0133 | -2.9 | -0.005 | -2.9 | 0.9976 |
| 20 | 0.9522 | -223.085 | -0.372 | 3568.795 | -6.2248 | -0.2758 | 3511.8 | 5.853 | -57.6 | 0.9528 |
| 40 | 0.9076 | -456.342 | -0.761 | 4391.733 | -7.8966 | -0.5710 | 4281.6 | 7.136 | -113.7 | 0.9090 |
| 60 | 0.8687 | -695.169 | -1.159 | 4867.521 | -9.0103 | -0.8796 | 4711.0 | 7.852 | -167.4 | 0.8689 |
| 80 | 0.8383 | -931.197 | -1.552 | 5196.194 | -9.8912 | -1.1892 | 5003.5 | 8.339 | -217.7 | 0.8330 |
| 100 | 0.8189 | -1153.697 | -1.923 | 5439.483 | -10.6290 | -1.4838 | 5223.7 | 8.706 | -263.4 | 0.8017 |
| 120 | 0.8109 | -1353.791 | -2.256 | 5625.793 | -11.2572 | -1.7500 | 5400.5 | 9.001 | -303.8 | 0.7749 |
| 140 | 0.8132 | -1527.760 | -2.546 | 5772.123 | -11.7955 | -1.9822 | 5549.5 | 9.249 | -338.5 | 0.7527 |
| 160 | 0.8239 | -1675.341 | -2.792 | 5889.484 | -12.2583 | -2.1798 | 5679.6 | 9.466 | -367.5 | 0.7346 |
| 180 | 0.8453 | -1786.857 | -2.978 | 5980.932 | -12.6391 | -2.3267 | 5796.6 | 9.661 | -390.8 | 0.7204 |
| 200 | 0.8740 | -1870.773 | -3.118 | 6054.608 | -12.9587 | -2.4371 | 5904.4 | 9.841 | -408.5 | 0.7097 |
| 220 | 0.9067 | -1935.806 | -3.226 | 6116.612 | -13.2355 | -2.5246 | 6005.5 | 10.009 | -421.0 | 0.7023 |
| 240 | 0.9420 | -1987.147 | -3.312 | 6170.454 | -13.4807 | -2.5970 | 6101.3 | 10.169 | -428.9 | 0.6977 |
| 260 | 0.9786 | -2028.054 | -3.380 | 6218.280 | -13.7015 | -2.6588 | 6192.8 | 10.321 | -432.7 | 0.6955 |
| 280 | 1.0163 | -2060.685 | -3.434 | 6261.482 | -13.9026 | -2.7128 | 6280.9 | 10.468 | -433.0 | 0.6953 |
| 300 | 1.0545 | -2086.544 | -3.478 | 6301.011 | -14.0875 | -2.7607 | 6366.0 | 10.610 | -430.1 | 0.6970 |
| 350 | 1.1515 | -2128.137 | -3.547 | 6387.801 | -14.4941 | -2.8612 | 6568.3 | 10.947 | -411.4 | 0.7080 |
| 400 | 1.2492 | -2145.008 | -3.575 | 6462.236 | -14.8402 | -2.9421 | 6799.1 | 11.265 | -379.7 | 0.7271 |

* Saturation pressure.

Table IX. Compressibility Factors from Corresponding States

| T, K | P, atm | Z | | | | |
|------|--------|-----------------|-----------------|-----------|---------------------|------------------|
| | | CM ^a | DK ^b | This work | Pitzer ^c | LGH ^d |
| 400 | 3 | 0.9687 | 0.9686 | 0.9683 | 0.968 | 0.964 |
| | 6 | 0.9360 | 0.9358 | 0.9346 | 0.935 | 0.928 |
| | 15 | 0.8260 | 0.8254 | 0.8230 | 0.820 | 0.832 |
| 500 | 100 | 0.5944 | 0.5957 | 0.5852 | 0.582 | 0.582 |
| | 200 | 0.7688 | 0.7687 | 0.7714 | 0.760 | 0.757 |
| | 300 | 1.0158 | 1.0504 | 1.0179 | 1.020 | 1.004 |
| 600 | 100 | 0.8309 | 0.8275 | 0.8189 | 0.800 | 0.802 |
| | 200 | 0.8907 | 0.8904 | 0.8740 | 0.880 | 0.871 |
| | 300 | 1.0579 | 1.1361 | 1.0545 | 1.110 | 1.053 |

^a Canjar and Manning (6). ^b Das and Kuloor (12). ^c Pitzer (26); Pitzer et al. (27). ^d Lyderson et al. (24).

Table X. Second Virial Coefficients

| T, K | -B, cm ³ mol ⁻¹ | | |
|--------|---------------------------------------|-------|-----------|
| | Literature values | API | This work |
| 273.16 | 889 ^a | 786.0 | 899.9 |
| 303.16 | 699 ^a | 608.2 | 687.4 |
| 344.26 | 457.2 ^b | 449.8 | 497.2 |
| 360.93 | 412.7 ^b | 402.6 | 441.2 |
| 377.59 | 374.0 ^b | 362.2 | 393.9 |
| 394.26 | 341.1 ^b | 327.1 | 353.4 |
| 406.87 | 318.3 ^b | 303.6 | 326.5 |
| 410.93 | 311.5 ^b | 296.5 | 318.5 |
| 444.26 | 259.6 ^b | 245.7 | 261.9 |
| 477.6 | 230.2 ^c | 205.2 | 218.1 |
| 510.9 | 191.6 ^c | 172.2 | 183.7 |

^a Jessen and Lightfoot (22). ^b Connolly (9). ^c Gunn (20).

The present PVT surface was not constrained by the critical conditions

$$\left(\frac{\partial P}{\partial \rho}\right)_{T_c} = 0 = \left(\frac{\partial^2 P}{\partial \rho^2}\right)_{T_c} \quad (7)$$

However, the constants of Table VII for the first region yield $(\partial P_r / \partial \rho_r)_{T(r=1)} = 0.0136$ and $(\partial^2 P_r / \partial \rho_r^2)_{T(r=1)} = 0.3055$.

Acknowledgment

Special thanks go to Bruno J. Zwolinski for his assistance in the preparation of the manuscript.

Nomenclature

- A = Helmholtz energy, cal mol⁻¹
- A₀, B₀, C₀, a, b, c, α, γ = BWR constants in atm cm³ K⁻¹ mol⁻¹ units (4)
- B = second virial coefficient, cm³ mol⁻¹
- CP = critical point, 408.13K
- f = fugacity, atm
- G = Gibbs energy, cal mol⁻¹
- H = enthalpy, cal mol⁻¹
- K = constants of Equation 5
- NBP = normal boiling point, 261.32K
- n = number of data points in a given region
- P = pressure, atm
- R = gas constant, 82.05606 atm cm³ K⁻¹ mol⁻¹
- N = total number of regions
- S = entropy, cal K⁻¹ mol⁻¹
- T = temperature, K

- Z = compressibility factor
- V = specific volume, cm³ mol⁻¹

Greek Letters

- λ = latent heat of vaporization, cal mol⁻¹
- θ = dimensionless temperature variable defined by Equation 3
- θ* = density and temperature-dependent factors defined in Equation 5
- ρ_{SL} = density, g cm⁻³ in Equation 3
- ρ = density, mol cm⁻³ in Equation 5
- ρ_L = limiting density constant in Equation 3
- φ = P - RTρ, atm

Superscripts

- I = ideal gas state
- ° = standard state; ideal gas at 1 atm and temperature, T
- * = indicates difference between quantity in region i and the value of that quantity at the region i - 1/region i interface

Subscripts

- c = critical point value
- j = running index for BWR terms
- r = divided by critical value
- r = region
- s = saturated property
- SV = saturated vapor
- SL = saturated liquid
- T_L = limiting temperature constant in Equation 3

Literature Cited

- (1) Aston, J. G., Kennedy, R. M., Schumann, S. C., *J. Amer. Chem. Soc.*, **62**, 2059, (1940).
- (2) Beattie, J. A., Edwards, D. G., Marple, S., *J. Chem. Phys.*, **17**, 576 (1949).
- (3) Beattie, J. A., Marple, S., Edwards, D. G., *ibid.*, **18**, 127 (1950).
- (4) Benedict, M., Webb, G. B., Rubin, L. C., *ibid.*, **8**, 334 (1940).
- (5) Benoitel, R. W., MS thesis, Pennsylvania State University, University Park, Pa., 1941.
- (6) Canjar, L. N., Manning, F. S., *Hydrocarbon Process.*, **42** (8), 127 (1962).
- (7) Carney, S. C., *Petrol. Refiner.*, **21** (9), 274 (1942).
- (8) Coffin, C. C., Maass, O., *J. Amer. Chem. Soc.*, **50**, 1427 (1928).
- (9) Connolly, J. F., *J. Phys. Chem.*, **66**, 1082 (1962).
- (10) Cragoe, C. S., *Nat. Bur. Stand.*, LC-736 (1943).
- (11) Dana, L. I., Jenkins, A. C., Burdick, J. N., Timm, R. C., *Refrig. Eng.*, **12**, 387 (1926).
- (12) Das, T. R., Kuloor, N. R., *Indian J. Technol.*, **5**, 40 (1967).
- (13) Davis, B. W., Rice, O. K., *J. Chem. Phys.*, **47**, 5043 (1967).
- (14) Eubank, P. T., Fort, B. F., *Can. J. Chem. Eng.*, **47**, 177 (1969).
- (15) Foehr, E. G., Fenske, M. R., *Ind. Eng. Chem.*, **41**, 1956 (1949).
- (16) Gilmour, J. B., Zwicker, J. O., Katz, J., Scott, R. L., *J. Phys. Chem.*, **71** (10), 3259 (1967).
- (17) Gilliland, E. R., Scheeline, H. W., *Ind. Eng. Chem.*, **32**, 48 (1940).
- (18) Grunberg, A. H., Nissan, A., *Trans. Faraday Soc.*, **44**, 1013 (1948).
- (19) Guggenheim, E. A., *J. Chem. Phys.*, **13**, 253 (1945).
- (20) Gunn, R. D., MS thesis, University of California, Berkeley, Calif., 1958.
- (21) Harand, J., *Monatsh. Chem.*, **65**, 153 (1935).
- (22) Jessen, F. W., Lightfoot, J. H., *Ind. Eng. Chem.*, **30**, 312 (1938).
- (23) Kudchadker, A. P., Alani, G. H., Zwolinski, B. J., *Chem. Rev.*, **68**, 659 (1968).
- (24) Lyderson, A. L., Greenkorn, R. A., Hougen, O. A., Generalized Thermodynamic Properties of Pure Liquids, University of Wisconsin College of Engineering, Rept. 4, October 1955.
- (25) Morris, W. M., Sage, B. H., Lacey, W. N., *Amer. Inst. Mining Met. Eng.*, Tech. Publ. No. 1128 (1939).
- (26) Pitzer, K. S., *J. Amer. Chem. Soc.*, **77**, 3427 (1955).
- (27) Pitzer, K. S., Lippmann, D. Z., Curl, R. F., Huggins, C. M., Peterson, D. E., *ibid.*, p 3433.
- (28) Sage, B. H., Lacey, W. N., *Ind. Eng. Chem.*, **30**, 673 (1938).
- (29) Seibert, F. M., Burrell, G. A., *J. Amer. Chem. Soc.*, **37**, 2683 (1915).
- (30) "Selected Values of Properties of Hydrocarbons and Related Compounds," API Research Project 44, Thermodynamics Research Center, Texas A&M University, College Station, Tex. (loose-leaf data sheets, extant, 1971).
- (31) Sliwinski, P., *Z. Phys. Chem. (Frankfurt am Main)*, **63**, 263 (1969).
- (32) Technical Committee, National Gasoline Association of America, *Ind. Eng. Chem.*, **34**, 1240 (1942).

- (33) Van der Vet, A. P., *Congr. Mond. Petrole*, 2^e, Paris II Sect. 2, 515 (1937).
- (34) Wackher, R. C., Linn, C. B., Grosse, A. V., *Ind. Eng. Chem.*, 37, 464 (1945).
- (35) Wilhoit, R. C., Hathaway, A. W., Tables of Conversion Factors Based on Accepted Constants as of 1965, Report of Investigation, API Research Project 44, Thermodynamics Research Center, Texas A&M University, College Station, Tex., 1965.

Received for review November 22, 1972. Accepted April 2, 1973. The support of the American Petroleum Institute Research Project 44 of the

Thermodynamics Research Center is acknowledged, together with that of Texas Engineering Experiment Station, both of Texas A&M University. **Supplementary Material Available.** The complete Table VIII will appear following these pages in the microfilm edition of this volume of the journal. Photocopies of the supplementary material from this paper only or microfiche (105 × 148 mm, 20× reduction, negatives) containing all of the supplementary material for the papers in this issue may be obtained from the Journals Department, American Chemical Society, 1155 16th St., N.W., Washington, D.C. 20036. Remit check or money order for \$3.00 for photocopy or \$2.00 for microfiche, referring to code number JCED-73-253.

Heat of Mixing and Vapor-Liquid Equilibrium of Acetophenone-2-Butanol System

Kenneth J. Miller¹ and Jiann-long Wu

Department of Chemistry, Northeast Louisiana University, Monroe, La. 71201

The heat of mixing of the acetophenone-2-butanol system exhibits an endothermic maximum of 541 cal/mol of solution close to 0.50 mole fraction at temperatures close to 25°C. Vapor-liquid equilibrium data of this system are reported at 1 atm pressure over the entire composition range.

The acetophenone-2-butanol system can be expected to deviate from ideality owing to hydrogen bonding between both like and unlike species. This work is part of a continuing study of phase equilibria and heat of mixing of alcohol-ketone systems. The heat of mixing absorbed in this system indicates the degree of the formation of alcohol-ketone hydrogen bonds with the loss of alcohol-alcohol hydrogen bonds, with the endothermic heat of mixing indicating a net decrease in number of hydrogen bonds. Activity coefficients calculated from the vapor-liquid equilibria data of this system also indicate solution nonideality.

Experimental

Details of the apparatus and the experimental methods used in this work have been described (2, 6). The 2-butanol used was reagent grade, obtained from Eastman Kodak Co., acetophenone used was chromatography, obtained from Matheson Coleman & Bell. Reagents were purified by fractional distillation. Boiling points and refractive indices at 25°C of 2-butanol and acetophenone used were 99.5°C and 1.3946 and 202.1°C and 1.5313, respectively. Equilibrium data were obtained by use of an improved Othmer still, and refractive index measurements were used for analysis. The overall reliability of equilibrium data is estimated to be ±0.005 mole fraction.

The calorimeter consisted of a 500-cm³ Dewar flask fitted with a Beckman and a standardized calorimetric thermometer and a stirrer. Liquids were mixed in all cases by crushing a thin-walled bulb of a capsule containing one component against the bottom of the Dewar flask which contained the other component. Heat capacity of the system was determined by passing a known current through a calibrated resistance wire which was wound about the glass stirrer. The power supply used was a Kepco unit, Model 430D, and was voltage regulat-

ed. The calorimeter was warmed prior to mixing to give a temperature change with an average temperature of 25°C.

Results and Discussion

Experimental results are shown in Figures 1 and 2 and tabulated in Tables I and II. The activity coefficients calculated and shown in Table I indicate considerable nonideality. The latter nonideality is supported by the heat of mixing absorbed for the system at 25°C as seen in Figure 2, which exhibits a maximum of 541 cal/mol of solution at approximately 0.5 mole fraction.

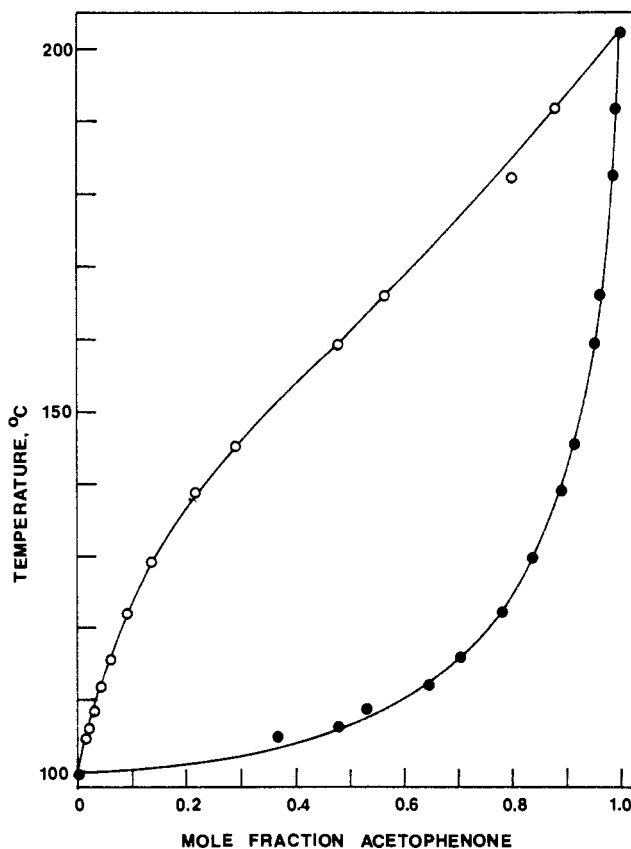


Figure 1. Boiling point-composition curve for acetophenone-2-butanol system

¹ To whom correspondence should be addressed.